## **AN INEXACT SCIENCE:**

### MEASUREMENT ERROR IN MODE AND LOCATION CHOICE MODELS

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### **Outline**

- 1.
- 2.
- 3.
- 4.



"Although this may seem a paradox, all exact science is dominated by the idea of approximation. When a man tells you that he knows the exact truth about anything, you are safe in inferring that he is an inexact man ..." – Bertrand Russell



"Aggregate statistics can sometimes mask important information ..." – Ben Bernanke

### **Motivation #1: Is statistical uncertainty a first-order problem?**

Like transport models, macroeconomic models are **calibrated by adjusting parameters** in the underlying behavioural models to replicate observed data.

Calibration is an **ad-hoc process of matching "moments"**, where moments means a characteristic, or property, of a statistical distribution, e.g. the mean ("annual average daily traffic").

Usually, **calibration does not (formally) consider uncertainty** in model parameters. Recent research, however, subjects macroeconomic ("DSGE") models to formal statistical tests (<u>link</u>) and finds:

"Taken together, these findings cast serious doubt on the meaningfulness of parameter estimates for this DSGE, and on whether this specification represents anything structural about the economy.

Takeaway: In many models, statistical uncertainty may be a first-order problem.



### **Motivation #2: Are macroscopic transport models "insensitive"?**

- **Common refrain:** Macroscopic transport models are too insensitive.
- If this is true, then why? Implies that people's behaviour is more sensitive to changes in transport outcomes than the models assume.
- Where <u>might</u> such biases arise? Possible sources include but are not limited to:
  - *Model structure,* e.g. generation / distribution / mode choice / assignment steps are not "separable"; and/or
  - *Omitted variables*, e.g. factors that influence people's choices (like departure time) are not included; and/or
  - *Biased parameters*, e.g. inaccurately estimated due to endogeneity or <u>measurement error</u> ...

**Question:** Doesn't measurement error simply introduce random noise? Let's see!



### Zeitgeist: Of "iron laws", measurement error, and attenuation

- Hausman's "Iron law" (2001): In the presence of random ME "... the magnitude of the estimate is usually smaller than expected. It is also called `attenuation' in the statistics literature."
- Hutcheon et al. (2010) discuss ME in a medical context: "Regression dilution bias" is where "... random measurement error in the values of an exposure variable (X) causes an attenuation or "flattening" of the slope of the line ... between the X and an outcome (Y) of interest."
- In the last decade, some transportation studies allow for ME in travel-times. Walker et al. (2010), for example, considers differences between *self-reported* vis-à-vis *estimated* travel-times and concludes that not allowing for ME tends to underestimate people's value of time.

Takeaway: Random ME is *not* a neutral statistical process. Rather, it biases parameters towards zero.



## Zeitgeist: Visualising measurement error



**Source:** Hutcheon, J. A., Chiolero, A., & Hanley, J. A. (2010). Random measurement error and regression dilution bias. *BMJ*, *340*.

- **Top-left panel:** X is deterministic; ie zero measurement error ( $\beta = 1.00$ , s.e. 0.00)
- **Bottom-left panel:** X measured with small random error ( $\beta = 0.71$ , s.e. 0.31)
- **Bottom-left panel:** X measured will large random error ( $\beta = 0.38$ , s.e. 0.34)

Takeaway: Random ME "flattens" the slope.

**Footnote:** "Random" = no selection effects, e.g. publication bias or strategic misrepresentation.

## Potential sources of measurement error in commuting data

Consider the following (typical) situation:

- We know (1) the zones where people live / work and (2) the main mode of transport that they use to commute (e.g. from census data)
- We want to measure the travel-time and -distance involved in commuting between home and work zones (e.g. to use in the estimation of destination and mode choice models).

### • BUT we don't know:

- Precise home locations (within the origin zone)
- Precise work locations (within the destination zone)
- Route, including intermediate destinations, e.g. schools
- Exactly where drivers park their car (both at home and at work)
- Frequency of commute across the week
- Time-of-departure

These "unknowns" (and others) introduce ME into estimates of travel-times and –distances.



### Data: Model zones → Measurement error (Car)



## Focus on measurement error induced by uncertainty in workers' home location.

- Use Open Street Maps to sample 20 home locations within each zone (SA2) weighted by the population of meshblocks within individual SA2s.
- We then calculate car and PT travel-times from these 20 "home" locations to all other SA2s (centroids) → distribution of travel-times for each OD pair in our data.
- The figure to the left shows the paths taken for 20 car journeys from Chelmer – Graceville to Brisbane City.



### Data: Model zones → Measurement error (PT)



Focus on measurement error induced by uncertainty in workers' home location.

 The figure to the left shows the paths taken for 20 PT journeys from Chelmer

 Graceville to Brisbane City.



### **Data: Measurement error in car travel-times**



Note: Random sample of 200 observations (from a total of 49,793).

- Vertical axis measures the log of total commuting flows whereas horizontal axis measures car travel-times.
- For car travel-times, the pink market denotes the mean whereas the bars denote the (approximate) 95% confidence intervals (that is, plus and minus two standard deviations). This interval is defined by the sampled data.
- We observe a clear downwards association (black trend line) as well as considerable heterogeneity in measurement error, especially towards the lower right-hand corner.

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### **Data: Measurement error in PT travel-times**



- Similar story for PT.
- Blue oval highlights an observation with an unusually high mean travel-time that is also measured imprecisely (error bars).
- When treated deterministically (i.e. no ME), such observations are likely to exert considerable influence over the estimated coefficients.
- If we allow for ME, however, then the model can "shrink" the travel-time to accord better with other information (e.g. model and other data).

Note: Random sample of 200 observations (from a total of 49,793).

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## **Results: Estimated parameters increase in magnitude**

		Without measurement error				With measurement error				
	Model	А	В	С	D	А	В	С	D	
Car	$\mu_c$	-1.925 (0.011)	0.009 (0.025)	-0.103 (0.031)	-0.820 (0.102)	-5.881 (0.073)	-2.574 (0.063)	-2.003 (0.065)	-4.116 (0.106)	We present standardized coefficients, which denote
ΡΤ	$\mu_p$	4.267 (0.021)	(0.044)	3.876 (0.178)	4.215 (0.227)	(0.164) (0.164)	7.764 (0.135)	9.370 (0.318)	(0.100) 11.591 (0.305)	the effect of a one s.d. increase in travel-times.
	$\begin{array}{c} \zeta_i, \zeta_j \\ t^p_{ij} \times \zeta \\ \text{C.F.} \end{array}$	No No No	Yes No No	Yes Yes No	Yes Yes Yes	No No No	Yes No No	Yes Yes No	Yes Yes Yes	
	loo-ic R <sup>2</sup>	182,439 0.869	50,858 0.992	43,534 0.996	42,152 0.997	40,710 0.999	37,044 0.999	35,203 0.999	31,244 0.999	The loo-ic measures external model performance

**Table 1:** Regression results for mode share models as per Section 4.1. Columns 1–4 and 5–8 report results without and with measurement error, respectively. Model A includes only car and PT travel-times,  $t_{ij}^c$  and  $t_{ij}^p$ , respectively. Model B includes group-level effects for individual origins and destinations,  $\zeta_i$  and  $\zeta_j$ , respectively. Model C includes group-level interaction effects between  $t_{ij}^p$  and both  $\zeta_i$  and  $\zeta_j$ . Finally, Model D uses a control function ("C.F.") to address endogeneity in travel-times, including the residuals from a first stage in which  $t_{ij}^c$  and  $t_{ij}^p$  are regressed against the crow-flies distance between the centroids of *i* and *j*,  $Z_{ij}$ . All models use 49,793 observations; s.e. in parentheses.

Takeaway: The effect of car and PT travel-times on mode choice is much larger when we allow for ME

## **Results: Latent ("true") travel-times "emerge from the ether"**



- Dashed green vertical lines denote the
   20 sampled travel-times; the solid
   green vertical lines denotes the mean.
- The light-grey denotes the "lognormal" distribution of mean traveltimes implied by the sampled data (mean and variance).
- The dark-grey denote the estimated distribution of latent ("true") mean travel-times estimated by the model.

 $n_{ij}^{c} \sim \mathcal{B}(n_{ij}, \mu^{c} t_{ij}^{c*} + \mu^{p} t_{ij}^{p*} + \zeta)$  $t_{ij}^{c*} \sim \text{Logn}(t_{ij}^{c}, (s_{ij}^{c})^{2}) t_{ij}^{p*} \sim \text{Logn}(t_{ij}^{p}, (s_{ij}^{p})^{2})$ 

*Latent travel-times*  $(t_{ij}^{c*} and t_{ij}^{p*})$  are estimated as part of the Bayesian "multi-level" model.





- Measurement error (ME) is a potentially important source of bias in the estimation of mode and location choice models. **We should definitely take ME more seriously!**
- Correcting for ME tends to increase the magnitude of parameters (possibly by a lot). Implies people respond even more strongly to transport outcomes!
- Even when ME is unknown, estimating models that allow for ME can significantly improve model performance and yield less biased parameters. **Why wouldn't you allow for ME!?!**

**Suggestion:** Re-estimate the destination and mode choice models that are currently used in macroscopic transport models to allow for measurement error.



# THANK YOU AND QUESTIONS



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